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Some Observations on Accuracy of Abundance<br>Indices Derived from Research Vessel Surveys<br>by<br>M. D. Grossiein<br>National Marine Fisheries Service<br>Biological Laboratory<br>Woods Hole, Massachusetts USA

## Introduction

In order to help evaluate the cost-benefit ratio of surveys it is necessary to have some idea of the magnitude of change in stock size that is considered significant, as well as the magnitude of change we are able to detect and with what probability. Clearly one of the most important questions is whether surveys can measure changes in abundance with sufficient accuracy to permit meaningful assessment of the short-term affects of fishing. However I think it is important to remember that we are also concerned with long term changes involving not just a few priority species but the entire groundfish community. In general a lower level of accuracy probably would suffice for monitoring long term changes than in the case of assessment on a year-to-year basis. My principal aim here is to provide some information on what accuracy is possible with catch-per-haul statistics from research vessel surveys.

When considering accuracy of estimates, we must distinguish between statistical precision or sampling error (variance) and the more general concept of accuracy. That is, an estimate may be very precise in terms of a small variance but have a large bias, and therefore not be very accurate. In our problem we are mainly concerned about the possible biases in the survey abundance index (catch per standard haul) as a relative measure of absolute abundance. That is, we shall consider our index unbiased if there is a constant proportionality (catchability coefficient) between our relative abundance index and the true absolute abundance of the stock. Note however that in terms of estimating actual numbers in the population, our relative abundance index is always biased so long as the catchability coefficient is $<1$.

Evidence to be presented later suggests that the assumption of constant proportionality is not unreasonable for certain species and observed stock changes in the case of joint US-USSR surveys. Consequently the following data on precision of abundance indices from these surveys probably reflects the general order of accuracy obtainable in measures of change in absolute stock size. Admittedly we will be on firmer ground when we can estimate variability of catchability coefficients, by utilizing direct (camera, acoustic) measures of abundance in conjunction with trawling.

## Statistical characteristics of traw1 catch data

As is well known trawl catches are highly variable even within relatively restricted areas because fish are not uniformly distributed; and random trawl hauls result in a frequency distribution of catches which is highly skewed. A major consequence of this skewness is that the variance is generally much larger than the mean resulting in very imprecise (although unbiased) estimates of the mean, and even less reliable estimates of the variance itself, except with very large sample sizes. That is, the standard error associated with the variance is particularly susceptible to departures from normality, and without a reliable estimate of the variance of course it is not possible to calculate meaningful confidence limits about the mean.

A standard approach to this general problem is to stratify the population to be sampled into high and low density units or strata, and then sample randomly within individual strata within each of which skewness is then reduced. Control of variability in this manner is one of the primary advantages to be gained from the technique of stratified random sampling. However in the case of trawl catches, considerable skewness remains even after stratification. For example the variability of variance estimates for haddock trawl catches on U.S. surveys, reflects the fact that catches within individual strata are still highly skewed (Table 1). Sampling strata used in the surveys discussed here are shown in Figures 1 and 2.

Another well known approach is to try to find a transformation which normalizes the frequency distribution of variables. We have found that on the average, stratum variances of trawl catches are approximately proportional to the square of the mean, i.e. the standard deviation is proportional to the mean. This is true for haddock (Fig. 3) and for many other species as well. This relation indicates that a log transformation is appropriate, and such a transformation tends to normalize the data and stabilize the variance (i.e. make means and variances independent). Also the log transformation converts multiplicative effects into linear additive effects. In terms of our problem of estimating proportional changes in abundance, this means that linear changes on a log scale represent estimates of multiple or factor changes on the original scale. That is, the anti-log of the difference between two log means on the linear scale. The estimates of proportional change on the original scale are believed to be essentially unbiased in the statistical sense, but it should be noted that the re-transformed mean is a biased estimate of the true mean on the linear scale (an unbiased estimate is theoretically possible).

## Calculation of stratified mean and variance

The basic index of abundance dealt with here is the stratified mean catch per standard haul, calculated by weighting each stratum mean according to the proportional size (area) of the stratum relative to all strata in the set. The variance of a stratified mean is similarly derived by weighting each stratum variance in proportion to the stratum area and according to the number of hauls in the stratum.
Stratum means (catch/haul, pounds) and variances for haddock in three sampling strata on

| CRUISE | STRATUM 16 |  |  |  | STRATUM 19 |  |  |  | STRATUM 20 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | No. hauls | Mean | Variance | Std. deviation | No. hauls | Mean | Variance | Std. deviation | $\begin{aligned} & \text { No. } \\ & \text { hauls } \end{aligned}$ | Mean | Variance | Std. deviation |
| 63-05 | 7 | 41 | 2,740 | 52 | 4 | 126 | 22,442 | 150 | 3 | 7 | 52 | 7 |
| 63-07 | 7 | 101 | 4,330 | 66 | 4 | 291 | 66,992 | 259 | 4 | 115 | 33,379 | 183 |
| 64-01 | 10 | 41 | 857 | 29 | 7 | 147 | 37,875 | 194 | 5 | 37 356 | 1,322 | . 264 |
| 64-210 | 8 | 300 | 338,823 | 582 | 5 | 364 | 209,248 | 457 | 5 | 356 | 70,072 155,074 | 264 394 |
| 64-13 | 7 | 148 | 31,926 | 179 | 6 | 168 | 26,652 | 163 | 5 | 335 21 | 155,074 338 | 18 |
| 65-2 | 6 | 73 | 6,309 | 80 | 6 | 392 | 2 243,932 | 494 1421 | 5 | 618 | 188,942 | 435 |
| 65-510 | 8 | 405 | 682,555 | 826 | 6 | 800 | 2,019,784 | 1421 | 5 | 332 | 160,830 | 401 |
| 65-14 | 7 | 78 | 3,266 | 57 | 5 | 171 49 | 14,377 6,058 | 120 | 5 | 43 | 1,243 | 35 |
| 66-601 | 7 | 73 | 17,357 | 132 | 6 | 49 | 6,058 15,495 | 78 124 | 5 | 126 | 11,584 | 108 |
| 66-614 | 7 | 62 | 1,423 | 38 | 6 | 54 | 15,495 | 124 | 6 | 37 | 4,140 | 65 |
| 67-721 | 8 | 14 | 564 | 24 | 9 | 52 | 4,096 | 34 | 6 | 13 | 4,351 | 19 |
| 68-803 | 9 | 49 | 5,533 | 74 | 8 | 42 | 1,189 | 34 | 6 | 25 | 3,574 | 60 |
| 68-817 | 8 | 19 | 2,850 | 53 | 9 | 0 | 1.831 | 43 | 6 | 3 | 3,51 | 6 |
| 69-902 | 14 | 71 | 26,570 | 163 | 8 | 45 | 1,831 | 43 | 6 | 23 | 2,610 | 51 |
| 69-908 | 10 | 7 | 185 | 14 | 9 | 6 | 124 | 11 | 6 | 16 | 2,610 | 34 |
| 69-911 | 12 | 4 | 117 | 11 | 9 | 7 | 413 | 20 | 6 | 16 | 1,136 | 9 |
| 70-703 | 10 | 130 | 120,926 | 348 | 8 | 11 | 409 | 20 | 5 | 5 |  |  |

Table 1

Computational formulae are:

$$
\begin{aligned}
& \bar{y}_{s t}=\frac{1}{N} \sum_{h} N_{h} \bar{y}_{h} \\
& v\left(\bar{y}_{s t}\right)=\frac{1}{N^{2}} \sum_{h} \frac{N_{h}^{2} S_{h}^{2}}{n_{h}}
\end{aligned}
$$

where $\bar{y}_{s t}$ and $V\left(\bar{y}_{s t}\right)$ are the stratified mean catch per haul and its variance respectively, of some set of strata, and

$$
\begin{aligned}
N_{h} & =\text { area of the } h^{\text {th }} \text { stratum } \\
N & =\sum_{h} N_{h}=\text { total area of all strata in the set } \\
\bar{y}_{h} & =\text { mean catch per haul in the } h^{t h} \text { stratum } \\
n_{h} & =\text { number of standard hauls in } h^{\text {th }} \text { stratum } \\
S_{h}^{2} & =\text { variance of catches in the } h^{t h} \text { stratum } \\
& \text { Examples of precision on linear scale }
\end{aligned}
$$

It is of interest to look at some examples of sampling errors of stratified means on a non-transformed scale before proceeding on to the log scale. Recall that in the examples of haddock data for individual strata, the standard deviation was on the average about equal to the mean (Fig. 3, Table 1). That is, coefficients of variation (ratio of standard deviation to the mean) were on the order of 100 percent with $5-7$ hauls per sample. In the case of stratified means for haddock on Georges Bank (representing about 60 hauls in strata $13-25$ combined) the average CV is only about 25 percent (Table 2). Similar values were obtained for cod.

In spite of the observed variability in estimates of individual stratum variances, we note that the CV's of the stratified means are reasonably consistent from year to year suggesting that the estimates of $V\left(\bar{y}_{s t}\right)$ may be approximately correct. Essentially we have computed a weighted mean of variances from 13 strata, and since most of these strata appear to have about the same variance this would account for the consistency among estimates of $V\left(\bar{y}_{s t}\right)$.

Stratified means for yellowtail on Georges Bank show CV's similar to those for cod and haddock (Table 3). Also shown in Table 3 are stratified means for the three principal strata for yellowtail, lepresenting about half of the total area of the strata set, 13-25. The CV's are only slightly greater on average for this subset of strata than for the entire set, although there were less than half as many hauls in the subset. Very little information on yellowtail was gained by sampling outside these three principal strata.

## Examples of precision on log scale

On the log scale the variances are nearly stabilized and the CV's of stratified means are on the order of $10-15$ percent for the same species and strata (Table 4). However note that now we are interested in the absolute rather than relative size of the standard deviation. For haddock $\pm 2$ S.D.'s ( $\pm .40$ ) corresponds to $\pm 50$ percent on the linear scale. Thus there is no great improvement in

Stratified mean catch per haul (pounds, linear) of cod and haddock on Georges Bank, (strata 13-25), and estimates of precision. Albatross IV fall surveys.

| Year | COD |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Variance | S.D. | S.D./Mean | $\begin{aligned} & \text { Mean } \pm \\ & 2 \text { S.D. } \end{aligned}$ |
| 1963 | 24.18 | 43.35 | 6.58 | . 27 | 11.0-37.3 |
| 1964 | 15.74 | 20.89 | 4.57 | . 29 | 6.6-24.9 |
| 1965 | 15.90 | 26.04 | 5.10 | . 32 | 5.7-26.1 |
| 1966 | 11.10 | 5.87 | 2.42 | . 22 | 6.3-15.9 |
| 1967 | 18.43 | 17.85 | 4.22 | . 23 | 10.0-26.9 |
| 1968 | 11.66 | 8.54 | 2.92 | . 25 | 5.8-17.5 |
| 1969 | 10.91 | 4.79 | 2.19 | . 20 | 6.5-15.3 |
|  | HADDOCK |  |  |  |  |
| 1963 | 112.83 | 590.75 | 24.30 | . 22 | 64.2-161.4 |
| 1964 | 165.68 | 1032.11 | 32.13 | . 19 | 101.4-229.9 |
| 1965 | 123.66 | 411.58 | 20.29 | . 16 | 83.1-164.2 |
| 1966 | 47.22 | 99.39 | 9.97 | . 21 | 27.3-67.2 |
| 1967 | 44.05 | 103.86 | 10.19 | . 23 | 23.7-64.4 |
| 1968 | 20.53 | 52.18 | 7.22 | . 35 | 6.1-35.0 |
| 1969 | 12.70 | 16.62 | 4.08 | . 32 | 4.5-20.9 |

Table 2

Stratified mean catch per haul (pounds, linear) of yellowtail on Georges Bank, and estimates of precision. Albatross IV fall surveys.

| Year | STRATA 13-25 (15,300 sq. miles) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Variance | S.D. | S.D./Mean | $\begin{aligned} & \text { Mean } \pm \\ & 2 \text { S.D. } \end{aligned}$ | No. hauls |
| 1963 | 18.00 | 11.56 | 3.40 | . 19 | 11.2-24.8 | 57 |
| 1964 | 28.58 | 53.27 | 7.30 | . 39 | 4.0-33.2 | 63 |
| 1965 | 12.36 | 15.73 | 3.97 | . 32 | 4.4-20.3 | 66 |
| 1966 | 5.38 | 3.07 | 1.75 | . 32 | 2.1-8.6 | 67 |
| 1967 | 9.71 | 6.91 | 2.63 | . 27 | 4.4-15.0 | 65 |
| 1968 | 14.73 | 11.33 | 3.37 | . 23 | 8.0.21.5 | 62 |
| 1969 | 12.02 | 9.73 | 3.12 | . 26 | 5.8-18.3 | 66 |
| 1970 | 6.37 | 3.49 | 1.87 | . 29 | 2.6-10.1 | 70 |
|  | STRATA $13,16,19$ (7,800 sq. miles) |  |  |  |  |  |
| 1963 | 23.10 | 33.19 | 5.76 | . 25 | 11.6-34.6 | 16 |
| 1964 | 32.10 | 194.97 | 13.96 | . 43 | 4.2-60.0. | 18 |
| 1965 | 18.48 | 56.99 | 7.55 | . 41 | 3.4-33.6 | 19 |
| 1966 | 8.71 | 11. 35 | 3.37 | . 39 | 2.0-15.4 | 19 |
| 1967 | 16.58 | 25.96 | 5.10 | . 31 | 6.4-26.8 | 25 |
| 1968 | 24.50 | 40.78 | 6.38 | . 26 | 11.7-37.3 | 25 |
| 1969 | 21.44 | 36.96 | 6.08 | . 28 | 9.3-33.6 | 30 |
| 1970 | 10.69 | 12.44 | 3.53 | . 33 | 3.6-17.8 | 24 |

Table 3

Stratified mean catch per haul (lb., $\log _{e}$ scale) and mcasures ' precision for selected species. Albatross IV fall surveys, Strata 13-25

| FallCruise | YELLOWTATL |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Variance | S.D. | $\begin{aligned} & \text { S.D./ } \\ & \text { mean } \end{aligned}$ | $2 \text { S.D. }$ | $\begin{aligned} & \text { Mean } \pm \\ & 2 \text { S.D. } \end{aligned}$ | $\begin{aligned} & \text { Factor } \\ & \text { diff. } \end{aligned}$ |
| 63-7 | 1.97 | . 026805 | . 1637 | . 08 | . 33 | 1.64-2.30 | 1.9 |
| 64-13 | 1.41 | . 037142 | . 1927 | . 14 | . 38 | 1.03-1.79 | 2.1 |
| 65-14 | 1.32 | . 029119 | . 1706 | . 13 | . 34 | .98-1.66 | 2.0 |
| 66-14 | 0.96 | . .025860 | . 1608 | . 17 | . 32 | .64-1.28 | 1.9 |
| 67-21 | 1.32 | . 027724 | . 1665 | . 13 | . 33 | .99-1.65 | 1.9 |
| 68-17 | 1.40 | . 038260 | . 1956 | . 14 | . 39 | 1.01-1.79 | 2.2 |
| 69-11 | 1.35 | . 025200 | . 1587 | . 12 | . 32 | 1.03-1.67 | 1.9 |
| 70-6 | 0.96 | . 0204 | . 1428 | . 15 | . 28 | .68-1.24 | 1.8 |
| H A D D O C K |  |  |  |  |  |  |  |
| 63-7 | 3.34 | . 052176 | . 2284 | . 07 | . 46 | 2.88-3.80 | 2.5 |
| 64-13 | 3.86 | . 080315 | . 2834 | . 07 | . 57 | 3.29-4.43 | 3.1 |
| 65-14 | 4.02 | . 042355 | . 2058 | . 05 | . 41 | 3.61-4.43 | 2.3 |
| 66-14 | 2.43 | . 044512 | . 2110 | . 09 | . 42 | 2.01-2.85 | 2.3 |
| 67-21 | 2.45 | . 052075 | . 2282 | . 09 | . 46 | 1.99-2.91 | 2.5 |
| 68-17 | 1.15 | . 029587 | . 1720 | . 15 | . 34 | 0.81-1.49 | 2.0 |
| 69-11 | 1.10 | . 021536 | . 1467 | . 13 | . 29 | 0.81-1.39 | 1.8 |
| 70-6 | 1.35 | . 0345 | . 1857 | . 14 | . 37 | 0.98-1.72 | 2.1 |
| COD |  |  |  |  |  |  |  |
| 63-7 | 1.75 | . 084829 | . 2912 | . 17 | . 58 | 1.17-2.33 | 3.2 |
| 64-13 | 1.29 | . 056270 | . 2372 | . 18 | . 47 | 0.82-1.76 | 2.6 |
| 65-14 | 1.32 | . 041737 | . 2043 | . 15 | . 41 | 0.91-1.73 | 2.2 |
| 66-14 | 1.20 | . 040673 | . 2017 | . 17 | . 40 | 0.80-1.60 | 2.2 |
| 67-21 | 1.74 | . 047301 | . 2175 | . 12 | . 44 | 1.30-2.18 | 2.4 |
| 68-17 | 1.04 | . 031888 | . 1786 | . 17 | . 36 | 0.68-1.40 | 2.1 |
| 69-11 | 1.32 | . 025381 | . 1593 | . 12 | . 32 | 1.00-1.64 | 1.9 |
| 70-6 | 1.35 | . 0332 | . 1822 | . 13 | . 36 | 0.99..1.71 | 2.1 |

[^0]the size of difference (proportional change on linear scale) we are able to detect as compared with the non-transformed scale, but we have more consistent estimates of those differences over the range of abundance levels, and the estimated confidence intervals more closely approximate true 95 percent fiducial limits. Results of stratified estimates for cod and haddock off western Nova Scotia are comparable to those on Georges Bank (Table 5).

The most significant feature of these data is that they indicate the present survey cannot detect with high probability proportional changes in abundance which are less than a factor of about 2. That is, the $\log _{e}$ difference between the lower and upper limits of the 95 percent C.I. is about 0.7 corresponding to a factor difference of 2 on the linear scale; and to be very sure that two means are significantly different there must be no overlap in the 95 percent confidence intervals.

## Sample size vs. precision

Some first approximations have been made of the relation between precision of stratified means and sample size (total number of haul The calculations are based on the general formula for estimating required sample size in stratified random sampling:

$$
n=\frac{\sum_{h} \frac{W_{h}^{2} S_{h}^{2}}{W_{h}}}{V+\frac{1}{N} \sum_{h} W_{h} s_{h}^{2}}
$$

and in terms of this problem,
$W_{h}$ and $S_{h}$ are as defined earlier,
$w_{h}=\frac{n_{h}}{n}$, the observed relative sampling effort in the
$h^{\text {th }}$ stratum (the ratio of the number of hauls in the $h^{\text {th }}$ stratum to the total number of hauls, $n$, in all strata of the specified set)
$V=$ desired variance of the stratified mean
$N=$ total number of possible hauls in the area represented by strata in the set.
Since the number of hauls in our survey is very small relative to the total number possible (strata $13-25$ cover roughly 15,000 square miles and each standard haul covers approximately. Ol square mile), the second term in the denominator is extremely small compared with the first. Thus,

$$
n \doteq \frac{1}{v} \Sigma \frac{W_{h}^{2} S_{h_{1}}^{2}}{w_{h}}
$$

Using the above formula and average values of $\mathrm{S}_{\mathrm{h}}{ }^{2}$ for haddock and $w_{h}$ based on eight Albatross IV fall surveys, estimates were made of the sample sizes required to achieve various levels of precision. For example, if we wanted to be able to detect proportional changes in abundance of $\pm 20$ percent with high probability, this would require an interval of $\pm_{2} S . D . ' s= \pm .18$ on the natural log scale, and thus S.D. $=.09$ and $V=.0081$. Substituting this value of $V$ in the above formula, $n=338$ hauls. Results of calculations for levels of precision between $10-100$ percent of the stratified mean for haddock are given in Table 6. The same computations for yellowtail in strata 13, 16, and 19 (representing about half of Georges Bank) are also shown in Table 6.

Stratified mean catch per haul (loge pounds) and variance esti For cod and haddock off western Nova Scotia. Albatross IV fal surveys in strata 31-35, 41, 42.

| Fall <br> ruise | HADDOCK |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | Variance | S.D. | S.D./ mean | 2 S.D. | 95\% CI | $\begin{gathered} \text { Factor } \\ \text { diff. } \end{gathered}$ |
| 5-14 | 3.61 | . 1918 | .4379 | . 12 | . 88 | 2.73-4.49 | 5.8 |
| 6-614 | 3.22 | . 1321 | . 3634 | . 11 | . 73 | 2.50-3.94 | 4.3 |
| 7-721 | 3.87 | . 1073 | . 3276 | . 08 | . 66 | 3.21-4.53 | 3.7 |
| 8-817 | 2.93 | . 0598 | . 2445 | . 08 | . 49 | 2.45-3.41 | 2.7 |
| 9-911 | 2.68 | . 0593 | . 2435 | . 09 | . 49 | 2.20-3.16 | 2.7 |
| $0-706$ | 2.82 | . 0352 | .1876 | . 07 | . 38 | 2.44-3.20 | 2.1 |

COD

| 5-14 | 3.25 | . 1492 | . 3863 | . 12 | . 77 | 2.47-4.03 | 4.7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6-614 | 2.71 | . 1608 | . 4010 | . 15 | . 80 | 1.91-3.51 | 5.0 |
| 7-721 | 2.16 | . 1051 | . 3242 | . 15 | .65 | 1.52-2.80 | 3.7 |
| 8-817 | 1.86 | . 0949 | . 3080 | . 16 | . 62 | 1.24-2.48 | 3.5 |
| 9-911 | 1.74 | . 0887 | . 2978 | . 17 | . 60 | 1.14-2.34 | 3.3 |
| 0-706 | 1.77 | . 0500 | . 2236 | ‘. 13 | . 45 | 1.32-2.22 | 2.5 |

Table 5

First approximations to sample sized (total number hauls) required for specified precision of stratified mean abundance indices ( $\log _{e}$ catch/haul in pounds) from Albatross IV surveys on Georges Bank. $1 /$

| LEVEL OF PRECISION |  | Total number hauls required, approximately proportional allocation Haddock Yellowtail |  |
| :---: | :---: | :---: | :---: |
| Percentage change linear scale | 2 standard deviations, linear scale |  |  |
|  |  | e (strata | rata 1 |
| $\pm 10 \%$ | $\pm .10$ | >500 | >500 |
| $\pm 20 \%$ | $\pm .18$ | 338 | 253 |
| $\pm 30 \%$ | $\pm .26$ | 164 | 120 |
| $\pm 50 \%$ | $\pm .40$ | 70 | 51. |
| $\pm 100 \%$ | $\pm .69$ | 23 | 17 |

1/ An empirical measure of the improvement in precision with increase in san ple size was obtained on the 1971 spring groundfish survey by pooling results of two cruises on Georges Bank, one in March and one in May. The pooled data shown below represent an increase in numbers of hauls of about 50 percent over the standard sampling rate, and resulted in reductions in standard deviations of about the magnitude predicted by the analysis based on the 1963-70 series of cruises shown above.
--Spring 1971 groundfish survey.


These data suggest that the cost of detecting with high probability changes of stock size as small as $\pm 10$ percent would be extremely high. It is even doubtful that we could justify the cost of measuring changes within $\pm 20$ percent; to get to this level it would appear that for haddock we would need to make nearly 5 times as many hauls as in the current survey which employs about 65 hauls in strata $13-25$ and achieves a precision of roughly $\pm 50$ percent (Table 6). In sampling for yellowtail it would appear that we would need almost as many hauls for strata 13, 16, and 19 alone, in order to obtain comparable levels of precision.

These results should be considered as first approximations since we have not fully investigated all of the characteristics of these data. For example it is possible that some improvement could be achieved with a modified log transformation which would further improve normalization of the data. Also it is possible that we could make significant gain in precision by additional stratification according to time of day, for those species exhibiting strong diurnal variations in availability. Additional stratification would cost something however, either in terms of fewer degrees of freedom for estimating stratum means and variances, or additional time at sea, or both. Thus there is no guarantee that additional stratification would achieve a net gain in information per unit cost. Further it is possible that the region could be more effectively stratified, for example by utilizing additional information on bottom sediments relative to groundfish distribution. However this too could only result in slight gains so long as we are interested in many species distributed over a wide area.

I think the most promising approach lies in controling or at least monitoring the haul-to-haul performance of the trawl; for example we do not have a precise measure of groundspeed, nor do we know what variations occur in wingspread and headrope height. Even direction of tow relative to bottom currents may be important for some species.

Even after all such improvements are incorporated however, it seems clear to me that there cannot be any drastic change in the observed relation between precision and sample size. The hard fact is that in sampling organisms with highly contagious distributions, achieving high precision will require intensive sampling.

So far we have been considering the precision of a single mean. It is of course possible to combine seasonal means into a single annual index which would have a smaller variance. For example if the means of two surveys were averaged, the standard deviation of the resulting mean would be reduced by approximately a factor of 0.7 (assuming homogeneous variances for the original means). Thus if the separate standard deviations were on the order of . 2 (corresponding to a $\pm 50$ percent level of precision), the standard deviation of the combined mean would be about . 14 , corresponding to a $\pm 30$ percent precision level. Essentially the same precision would have been achieved by simply doubling the sampling effort on one cruise, and in that sense there would be no gain in accuracy through combination of two cruises. However by combining results of more than one season within a given year, there is less likelihood of bias due to variation in seasonal availability factors.

Finally it should be noted that in most cases it usually takes at least several years for major changes in stock size to occur. Given annual surveys, we then have a number of points in a time series with which to test for a significant slope or trend, and precision of such a test would be greater than that indicated for a single survey.

## Comparisons between research and commercial abundance indices

Returning now to the more general concept of accuracy, we need to consider further the problem of bias in conjunction with precision. In particular we are concerned about the possibility that the ratio of our relative abundance indices to the absolute (unknown) abundance may not be constant at difference levels of absolute abundance. We may gain some insight into this question by comparing abundance indices derived from both research and commercial catch data. However we must use care in making such comparisons because both types of data are subject to error. The commercial data are potentially more subject to serious bias, and research data are usually characterized by larger sampling errors.

Potential major sources of bias in the commercial data are 1) changes in the effective unit of effort usually related to economic or technological factors, and 2 ) possible variation in efficiency of what is thought to be a standard unit of effort, resulting from variations in availability of fish independent of absolute abundance (e.g. envirommentally controlled variations in aggregation). With proper sample design the research vessel index is free of the first bias, but still may be subject to bias from changes in availability. For example the catchability coefficient for a given species and research trawl may change due to a change in vertical distribution of the species, in response to some environmental factor or even as a function of absolute abundance itself. The possibility of a significant bias of this type intuitively would seem to be mach greater for a species for which the trawl has a very low efficiency. We shall return to this point later in comparing joint US..USSR survey results.

From the standpoint of piecision it is important to recognize that the commerial abundance index neariy always will be more precise than a research index simply because it is based on a very large number of hauls. However we seldow obtain variance estimates for commercial indices since at best it is a very complicated task involving many sour ces of error. It is a relatively simple matter to obtain statistically valid estinates of sampling error from surveys but unfortunately the erows are large.

With the above characteristios in mind we may now turn to some comparisons of research and comercial indices. Fourth quarter U.S. landings/day figures for cod, haddock, and yellowtail on Georges Bank, and U.S. fall survey abundance indices for strata 13-25, are tabulated for the period 1963.1969 in Table 7. The percentage deviations of each index from the 163.169 mean are plotted in Figure 4, and it is clear that the two indices are correlated for haddock and yellowtail

For yellowtail the commercial and research indices show quite similar trends in relative abundance; and the magnitude of changes indicated by the research indices was not much greater than that indicated by the commercial indices (rig. 4). Correlation coefficients were .95 (linear scale, survey) and 81 (log scale, survey), and both are significant ai the 95 percent probability level.

The correspondence is perhaps alwost too good in this case. Tr + is, if the research index is accurate to within only $\pm 50$ percent changes in abundance, then one wight not expect such close correspondence from year to year when the actual yellowtail abundance
Fourth quarter U.S. commercial abundance indices and Albatross fV fall survey indicos
for cod, haddock and yellowtail on Georges Bank. Commercial index: Landings/day
(1b. $x 10^{-3}$ ) $5 Z$ east. Survey index: stratified mean catch/haul ( $1 \mathrm{~b} .$, linear and $\log _{e}$ ) strata 13-25.

| YEAR | COD |  |  | H A D DOCK |  |  | YELLOWTAIL |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Comm. | Sur vey |  | Comm. | Survey |  | Comm. | Survey |  |
|  |  | 1 b . | $\log _{e} \mathrm{lb}$. |  | 1 b . | $\log _{e} 1 \mathrm{lb}$. |  | 1b. | $\log _{e} 1 \mathrm{~b}$. |
| 1963 | 2.1 | 25.1 | 1.8 | 8.2 | 118.6 | 3.3 | 8.7 | 21.6 | 2.0 |
| 1964 | 1.4 | 15.6 | 1.3 | 10.8 | 193.6 | 3.9 | 8.0 | 22.3 | 1.4 |
| 1965 | 0.8 | 7.5 | 1.3 | 14.9 | 131.0 | 4.0 | 7.3. | 14.7 | 1.3 |
| 1966 | 1.8 | 8.8 | 1.2 | 9.4 | 51.4 | 2.4 | 4.5 | 6.5 | 1.0 |
| 1967 | 2.5 | 20.0 | 1.7 | 5.7 | 43.1 | 2.4 | 6.1 | 11.7 | 1.3 |
| 1968 | 2.8 | 10.8 | 1.0 | 6.1 | 19.2 | 1.2 | 7.7 | 17.7 | 1.4 |
| 1969 | 5.1 | 7.5 | 1.3 | 4.8 | 5.6 | 1.1 | 6.1 | 14.4 | 1.4 |

Table 7
(based on fairly reliable commercial indices) appeared to vary by no more than about 30 percent from the mean. In other words there may be some indication here that variance estimates may be inflated. More detailed study will be required to clarify this notion.

For Georges Bank haddock correlation coefficients are also significant at the 95 percent level $=.74$ and .84 for linear and log scales respectively. Corresponding trends in abundance are indicated but the research indices show a much greater magnitude of change in stock size than is indicated by the U.S. commercial index. In this case however the commercial indices are believed to have been negatively biased particularly in the midu1960's as has been described by Hennemuth (1968). Another feature is that the efficiency of vessels remaining in the fishery after 1967 probably was above average, which might be the explanation for the apparent discrepancy in trend between the two sets of indices in the late 1960's. It should be emphasized that changes in efficiency of commercial fleets are quite likely when stock levels change drastically.

There is less consistency between commercial and research indices for Georges Bank cod than for yellowtail and haddock. Up to 1967 there was a rough similarity in trends, but thereafter the correspondence is poor (Fig. 4). Correlation coefficients do not differ significantly from zero. In the later years it is possible that the scarcity of haddock may have resulted in a partial shift of effort toward cod, in which case the commercial index would have a positive bias. This too will require more detailed study.

Another set of comparisons is provided by U. S. commercial and research indices for haddock off western Nova Scotia (Table 8). The best comparison is afforded by the first quarter comercial indices vs. the spring research indices and these show quite a consistent picture both with respect to trend and magnitude of change (Fig. 5). Trends are basically similar between fall surveys and annual commercial indices, but an unusually large discrepancy occurred in 1967. Sampling error was not particularly high in that year (see Table 5) and so far 1 have no explanation for the apparent discrepancy.

Still another set of conparisons is available for red hake in southern New England. During the perica 1965-1968 there was a rapid steady decline in abundance showu $b y$ both the catch per haul statistics of the USSR fleet and the $0 . S$ survey (Table 9, Fig. 6). The commercial data suggest that by 1968 abundance had dropped to about one-quarter the 1965 level, and the survey data impiy a decline to about one-third the 1965 level. Abundance appeared to increase again in 1969 as indicated by bcih comiaercial and research indices. In contrast to southern kew Engiand comparisons for Georges Bank show poor correspondence between the commercial and research data for red hake (Table 9, Fig. $\%$ ). This may be partly due to the fact that after 1965 the principal insing effort by the Soviet fleet on red hake occurred in soithein New England, and Georges Bank effort was not directed specifirally toward red hake.

To summarize briefly the comparisons zuong commercial and research indices, it appears that survey indices more often than not provide about the same tiends and reiative changes in stock size as do commercial indices. This ithink is basically encouraging. The problem now is hor to improve precision.

| ```and Albatross IV surveys. Commercial index: U.S. landings day, metric tons rd. fresh, Browns Banks Survey: stratified mean catch per haul (loge pounds), strata 31-35, 41, 42``` |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Commercial |  | Survey |  |
| Year | Annual | lst Qtr. | Fall | Spring |
| 1963 |  | 6.9 |  |  |
| 1964 | 7.5 | 6.9 | - | - |
| 1965 | 6.5 | 5.3 | 3.61 | - |
| 1966 | 4.7 | 6.8 | 3.22 | 3.72 |
| 1967 | 5.4 | 3.4 | 3.87 | - |
| 1968 | 4.5 | 3.3 | 2.93 | 3.13 |
| 1969 | 3.4 | 3.2 | 2.68 | . 2.53 |
| 1970 |  |  | 2.82 | 2.99 |
|  | - |  |  |  |

## Table 8

Abundance indices for red hake in New England waters based on catch $1 /$ por haul statistics from USSR fleet , and joint US_USSR groundfish 2/
surveys


1/ Catch pez haul hour for red hake from ICNAF research document $70 / 39$ by Richter, for "stocks I and II" which correspond approximately to strata sets $13-25$ and l-12 respectively.
2/ Stratified mean catch per haul (pounds, natural log scale).
3/ Estimate provided on graph by Dr. Noskov at Working Group in Copenhagen, January 1971.

Table 9

## Comparisons between U.S. and USSR survey indices

The larger USSR trawls appear to have up to 5 times the fishing pomert off the U.S. survey trawl for some species, as indicated by 4tawll comparisom experiments and joint surveys since 1967 (ICNAF Res, Der:"S. $8 / 86,70-80$ ). The question arises whether there is. andy sigmificanit rellation between fishing power and accuracy of the abumdiance fimdices. We have been particularly concerned about the prossiibriblityy that in the case of species for which our U.S. gear. has reliattively low fisining power (e.g. red and silver hake), Fellativelly minar cmanges in behavior and especially vertical diistaribuntion might change availability enough to obscure real athanges in abrmandince. So far there is no clear evidence of any such dijsaduanitage writh the smaller trawl from the standpoint of аясив:

Whith respect to sampling errors we find that variances of striatified mearns are fairly comparable for the two sizes of gear, andl they appeav to be rather independent of fishing power differentrialls. Fon example the fishing power differential is large for ned hake buit quitite small for cod, haddock, and yellowtail, and yet vaniances ane quite similar for all these species and both typers af thawl ir New England waters (Tables 10, 11). Generally similiad nesulits were obitained in the 1970 surveys off Nova Scotia (Thablle T2) !.

With, nespect to comparability of trends we find very close connespondence between, the indices for red hake in southern New Hngliand, in boith direction and magnitude (Fig. 6). The correspondence iss not as good for silver make in the southern New England arres bout the dijurectuion of change is the same from year to year
 fiforr hooth read and siditwert hable Georges Bank, where they were less aboundiantt, burtu aggain the cour respondemce was better for red hake (ffiiggs. 66, 7) ). Whesse data aw difficult to interpret because the
 $11968 \%$; the 1199699 geeary ppr chabllly buad gireater fishing power.

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Stratified mean catch per haul $\log _{e}$ pounds) of selected species in southern New England (strata l-12). U.S. and USSR joint surveys.

| YE.AR | Strat.mean |  | Variance |  | S. D. |  | S.D./mean |  | No. hauls |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR |
| 1067 | 1.05 | 2.07 | . 0229 | . 0554 | . 1513 | . 2354 | . 14 | . 11 | 65 | 40 |
| $1503_{2 /}$ | 0.79 | 1.88 | . 0238 | . 0421 | . 1543 | . 2052 | . 20 | . 11 | 62 | 46 |
| $190{ }^{-1}$ | 1.18 | 2.20 | . 0236 | . 0760 | . 1536 | . 2757 | . 13 | . 12 | 66 | 42 |
| 1970 | 1.35 | 2.36 | . 0199 | . 0314 | . 1411 | . 1772 | . 10 | . 08 | 64 | 56 |
| SILVER HAKE |  |  |  |  |  |  |  |  |  |  |
|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USS |
| 1967 | 1.63 | 2.64 | . 0202 | . 0579 | . 1421 | . 2406 | . 09 | . 09 |  |  |
| 1968 | 1.80 | 3.62 | . 0155 | . 0404 | . 1245 | . 2010 | . 07 | . 06 |  |  |
| 1969 | 1.20 | 3.38 | . 0142 | . 0676 | . 1192 | . 2600 | .10 | . 08 |  |  |
| 1970 | 1.35 | 3.71 | . 0125 | . 0273 | . 1118 | . 1652 | . 08 | . 04 |  |  |

YELLOWTATL

|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. USSR | U.S. USSR |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 2.25 | 1.70 | .0270 | .0514 | .1643 | .2267 | .07 | .13 |  |
| 1968 | 2.03 | 1.78 | .0380 | .0592 | .1949 | .2433 | .10 | .14 |  |
| 1969 | 2.00 | 1.75 | .0361 | .0708 | .1900 | .2661 | .10 | .15 |  |
| 1970 | 2.12 | 1.50 | .0420 | .0657 | .2049 | .2563 | .10 | .17 |  |

1/ No hauls in stratum 10; sampiing in strata 9, 11, 12 restricted to area west of $70^{\circ} \mathrm{W}$.

2/ 24.6 m trawl used by USSR vessel in 1969; 27.1 m trawl used by USSR vessels in all other surveys.

Table 10

Stratified mean catch per haul ( $\log _{e}$ pounds) of selected species in Gcorges Bank (strata 13-25. U.S. and USSR joint surveys.

| YEAR | COD |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean |  | Variance |  | S. D. |  | S.D./mean |  | No. hauls |
|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. USSR |
| $\begin{aligned} & 19671 / \\ & 1968 \frac{1 /}{} \\ & 1969 \frac{2 /}{3 /} \\ & 19703 / \end{aligned}$ | 1.74 | - | . 0473 | - | . 2175 | - | . 12 | - | 67 |
|  | 1.04 | 1.19 | . 0319 | . 0400 | . 1786 | . 2000 | . 17 | . 17 | 6949 |
|  | 1.32 | 1.59 | . 0254 | . 0178 | . 1594 | . 1334 | . 12 | . 08 | 73.37 |
|  | 1.35 | 0.87 | . 0332 | . 0367 | . 1822 | . 1916 | . 13 | . 22 | $70 \quad 31$ |
| HADDOCK |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & 1967 \\ & 1968 \\ & 1969 \\ & 1970 \end{aligned}$ | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. USSR |  | U.S. USSR |
|  | $\begin{aligned} & 2.45 \\ & 1.15 \\ & 1.10 \\ & 1.35 \end{aligned}$ | $\begin{aligned} & 1.07 \\ & 1.07 \\ & 1.65 \\ & 0.57 \end{aligned}$ | $\begin{aligned} & .0521 \\ & .0296 \\ & .0215 \\ & .0345 \end{aligned}$ | $\begin{aligned} & .0 \\ & .0248 \\ & .0649 \\ & .0285 \end{aligned}$ | $\begin{aligned} & .2282 \\ & .1720 \\ & .1466 \\ & .1857 \end{aligned}$ | - | $\begin{aligned} & .09 \\ & .15 \\ & .13 \\ & .14 \end{aligned}$ | $\begin{array}{r} . \\ .16 \\ .15 \\ .30 \end{array}$ |  |
|  |  |  |  |  |  | . 1667 |  |  |  |
|  |  |  |  |  |  | . 2548 |  |  |  |
|  |  |  |  |  |  | . 1688 |  |  |  |
| - | Y EL L O W TA L |  |  |  |  |  |  |  |  |
|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. USSR |
| 1967 | 1.32 | - | . 0277 | . - | . 1664 | - | . 13 | - |  |
| 1968 | 1.40 | 1.01 | . 0382 | . 0340 | . 1954 | . 1844 | . 14 | . 18 |  |
| 1969 | 1.35 | 1.91 | . 0252 | . 0615 | . 1587 | . 2480 | . 12 | . 13 |  |
| 1970 | 0.96 | 1.80 | . 0204 | . 0878 | . 1428 | . 2963 | . 15 | . 16 |  |

1/ No hauls in stratum 25; only one haul each in strata 15, 17 and 22. 2/ 24.6 m trawl used by USSR vessel in 1969; 27.1 m trawl used by USSR vessels in all other surveys.
3/ No hauls in strata $23-25$ by USSR vessel in 1970.

Table 11

| Stratified means (catch per haul, $\log _{e}$ pounds) and measures of precision for selectcd species in 1970 surveys in Division 4 X (sampling strata 31, 32, 41-49) <br> KVANT - 34 hauls $\quad$ ALBATROSS IV - 45 hauls |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Species | Stratified mean |  | Variance |  | S.D. |  | Mean | $\pm 2$ S.D. |  | $\begin{aligned} & \text { tor } \\ & \text { rence } \end{aligned}$ |
|  | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USSR | U.S. | USṠR |
| Cod | 1.20 | 0.55 | . 0690 | . 0416 | . 2627 | . 2040 | .68-1.72 | .15-. 95 | 2.9 | 2.2 |
| Haddock | 2.05 | 1.81 | . 0231 | . 0574 | . 1520 | . 2396 | 1.75-2.35 | 1.33-2.29 | 1.8 | 2.6 |
| Am. Dab | 0.83 | 0.21 | . 0214 | . 0041 | . 1463 | . 0640 | .53-1.13 | .09-. 33 | 1.8 | 1.3 |
| Yellowtail | 0.35 | 0.11 | . 0227 | . 0041 | . 1507 | . 0640 | .05-.65 | 0-. 23 | 1.8 | 1.3 |
| Silver hake | 0.85 | 1.02 | . 0216 | . 0941 | . 1470 | . 3068 | . 55-1.15 | .40-1.64 | 1.8 | 3.4 |

Table 12


Figure 1. Sampling sirata used fn 1970 joint US-USSR groundfish surveys from Cape Hatteras to Georges Bank.

100


Figure 2. Sampling strata usod in 1970 joint US-TISSR
survey on Nova Scotian shelf.


Figure 3. Soatter diagram of standard deviations and corresponding, stratified means for data shown in table 1.


Figure 4. U.S. Commercial va, survey abundance indices on Georges Bank.


Figure 5. U.S. Commeraial vs. survey abundance indioes for haddook in Division 4 X .


Figure 6. OSSR Commercial $\begin{aligned} & \text { (s. joint survey abundance } \\ & \text { indices for red hake. }\end{aligned}$

## SILVER HAKE ABUNDANCE INDICES



Figure 7. USSR Commeraial $\nabla$. indices fox silver hake.


[^0]:    Table 4

