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Estimating Pup Production and Population Size of the Northwest Atlantic Harp Seal (*Phoca groenlandica*).

by

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Abstract

Pup production and population size of Northwest Atlantic harp seals (*Phoca groenlandica*) for the period 1960 to 2000 were estimated using independent survey estimates of pup production, annual estimates of pregnancy rates, and age-structured removals. Removals included reported catch, estimated by-catch and assumed levels of seals killed but not landed (struck and lost). These data were fit to a three-parameter age structured population model that allows for differing assumptions of pup mortality. The two parameters estimated in the model are the pup selection parameter (s) and unaccounted mortality (m). The impact of assuming that the mortality of young seals (age class 0) was greater than that of seals one year of age and older (1+) was illustrated by using a fixed parameter (γ) as the ratio of age class 0 mortality to that of older seals. Replacement yields were estimated using differing assumptions of the age structure of the harvest. The uncertainty associated with the estimates was determined by randomly re-sampling from within the sampling error of the pup production estimates.

Assuming that the unreported mortality of age class 0 seals is 3 times that of 1+ animals, the total population was estimated to be approximately 5.2 million, with a 95% confidence interval of 4.0 to 6.4 million seals in 2000. Assuming different γ -values changes the estimates slightly, but differences were minimal. The population was estimated to have increased from less than 2 million in the early 1970s until 1996; since then the population has been relatively stable. Using the current age structure of the removals (~70% young of the year), the 2000 replacement harvest was estimated to be approximately 533,000, with 95% confidence interval (C.I.) 373,000, to 693,000. Assuming that the levels of by-catch and the Greenland harvest remain at their 1999 levels, and accounting for struck and lost, the corresponding replacement level of seals that can be landed in southern Canada at the proportion of pups observed in 1999 (90%) is 257,000; (95% C.I. 102,000, to 342,000). This level would be reduced slightly if the proportion of young in the harvest decreases.

Introduction

Various approaches have been used to estimate the size of the harp seal (*Phoca groenlandica*) population in the Northwest Atlantic (see Roff and Bowen, 1983 or Shelton *et al.*, 1996 for reviews of the different methods). Earlier estimates, based primarily on interpreting age composition data, use either the survival index approach (e.g. Sergeant, 1971; Winters, 1978; Cooke, 1985) or sequential population analysis (e.g. Lett and Benjaminsen, 1977; Winters, 1978). More recent efforts have focused upon fitting various forms of a two-parameter population model (variation of a Leslie model) to independent field estimates of pup production for several years (termed the population model approach, e. g. Roff and Bowen, 1983, 1986; Shelton *et al.*, 1992, 1996; Stenson *et al.*, 1999).

Shelton *et al.* (1996) estimated the population of Northwest Atlantic harp seals using the model described in Cadigan and Shelton (1993), which involved fitting a population model to independent estimates of pup production. With the exception of the methods used to obtain initial pup production and parameter estimation, the model used by Shelton *et al.* (1996) was very similar to that of Roff and Bowen (1983). Based upon annual estimates of age-specific reproductive rates and catch-at-age up to 1993 and six independent survey (mark-recapture and aerial) estimates of

pup production (1978, 1979, 1980, 1983, 1990 and 1994), total population was estimated to be approximately 4.8 million if the natural mortality was assumed to be constant across ages, and 4.5 million if the mortality rate of young of the year seals was assumed to be 3 times that of seals one year of age and older (1+). Warren *et al.* (1997) estimated that the 95% confidence intervals associated with the constant mortality model were 4.1 – 5.5 million. The population was then estimated to be growing at 5% per year.

Since 1996 Canadian catches increased dramatically from an average of 52,000 from 1983 - 1995 to over 240,000 during 1996 - 1999 (Stenson *et al.*, 2000a). Also, based on new methods of reporting catches, the estimates of removals in Greenland during the late 1980s and early 1990s were revised upward from the ~16,000 assumed in Shelton *et al.* 1996 to over 50,000 (Anon. 1999a). Similar to the Canadian catch, catches in Greenland continued to increase: over 53,000 seals were landed in 1993, compared to an estimated harvest of 103,000 in 1999, an average increase of 12% per annum (Stenson *et al.*, 2000a).

Stenson *et al.* (1999) explored the impact of these increased catches on the population estimates and estimated 1998 population size using reproductive and catch data up to 1998, but pup production data which terminated in 1994. They also estimated the impact of incorporating several assumed levels of struck and lost (i.e. seals that are killed but not landed and therefore not included in the reported landings). Reviewing these estimates, the National Marine Mammal Peer Review Committee (Anon 1999b) concluded that, based on the 1994 pup production survey, the population was on the order of 5 million, but that a new pup production survey was necessary in order to determine the current population size. The committee also recommended that future estimates be made with models that included variable mortality for different age classes and that as many sources of unreported mortality as possible be incorporated explicitly in the population model. The committee suggested that until additional information is available, future modeling assume that 5% of the total numbers of young of year killed in southern Canada are lost while 50% of older animals and all age classes in the northern areas (Arctic and Greenland) are not recovered.

Surveys were carried out in March 1999 to estimate pup production of harp seals in the Northwest Atlantic. Stenson *et al.* (2000b) estimated that 997,900 (SE=102,100) pups were born off Newfoundland and in the Gulf of St. Lawrence during 1999. Also, Walsh *et al.* (2000) estimated the numbers of seals caught incidentally in lumpfish fishing gear in Newfoundland since 1978 while Sjare and Stenson (2000) provided additional information on the levels of struck and lost in the Canadian commercial hunt.

The objective of this study is to estimate current population size of Northwest Atlantic harp seals using an age structured population model, incorporating recent estimates of reproductive rates (Sjare *et al.*, 2000), unreported mortality (Waring *et al.* 1999; Walsh *et al.* 2000; Sjare and Stenson, 2000), and pup production. Replacement yields (in units of total removals) and the corresponding levels of reported catch in the Canadian Front and Gulf that would provide such yields are calculated, assuming that other hunt components take the same number of animals as each component did in 1999. In addition, we present an estimate of population size in 2005 and 2010 if these replacement yields are taken in the intervening period. Uncertainty in these estimates was determined incorporating the error associated with the available pup production estimates.

Model Structure

The population model used to estimate numbers-at-age for harp seals in the Northwest Atlantic from 1960 to 2000 is an extension of the model described in Shelton *et al.* (1996) and Cadigan and Shelton (1993). The original model (hereafter referred to as the 'Cadigan-Shelton' model) consists of two components, the first being the population dynamics model while the second involves a statistical model. For comparative purposes, we present a description of both the Cadigan-Shelton model and the extended version used in this study.

The basic formulation of the Cadigan-Shelton model is:

$$n_{a,t} = (n_{a-1,t-1}e^{-m/2} - c_{a-1,t-1})e^{-m/2}$$

For $0 < a < A$,

$$n_{A,t} = (n_{A-1,t-1}e^{-m/2} - c_{A-1,t-1})e^{-m/2}$$

For $a = A$, where $A-1$ is taken as ages $A-1$ and greater, and

$$n_{a,t} = \sum_{a=1}^A n_{a,t} P_{a,t}$$

for $a = 0$;

where

- $n_{a,t}$ = population numbers-at-age a in year t ,
- $c_{a,t}$ = the numbers caught at age a in year t ,
- $P_{a,t}$ = per capita pregnancy rate of age a parents in year t ,
assuming a 1:1 sex ratio,
- m = instantaneous rate of natural mortality, and,
- A = the 'plus' age class (i.e. older ages are lumped into this age
class and accounted for separately, taken as age 12 in this
analysis).

In order to predict numbers-at-age for years prior to the first year for which continuous pregnancy data are available, it is assumed that the annual pup catch was a constant proportion (s) of the number of pups born ($s=(1/\text{exploitation rate})$). Thus, for years prior to the first year for which pregnancy data were available (year t_0);

$$n_{a,t_0-1} = se^{-ma} c_{0,t_0-a-1} - \sum_{i=1}^a e^{-m(i-1/2)} c_{a-i,t_0-i-1}$$

for $a = 1$ to \mathbf{A} where \mathbf{A} is a terminal (rather than a plus) age ($\mathbf{A}=25$ years in the formulations that follow). This equation is applied iteratively to go back in time and fill in the numbers-at-age matrix.

The modified form of the Cadigan-Shelton model below allows direct investigation of the impact of assuming that the mortality of age class 0 (m_0) is unequal to that of older seals (m_{1+}). The model has the ability to fix m_0 as a constant multiple of m_{1+} . We denote this multiple as γ (i.e. $m_0 = \gamma m_{1+}$). In general, mammalian biology suggests that γ is greater than or equal to 1.

The modified model has the form:

$$n_{a,t} = n_{a-1,t-1}e^{-(g)m} - c_{a-1,t-1}e^{-(g)m/2}$$

for $a=1$

$$n_{a,t} = (n_{a-1,t-1}e^{-m/2} - c_{a-1,t-1})e^{-m/2}$$

for $1 < a < A$,

$$n_{A,t} = (n_{A-1,t-1}e^{-m/2} - c_{A-1,t-1})e^{-m/2}$$

for $a = A$, where $A-1$ is taken as ages $A-1$ and greater, and

$$n_{a,t} = \sum_{a=1}^A n_{a,t} P_{a,t}$$

for $a = 0$, where the variables and subscripts have the same definitions as in the Cadigan-Shelton model. The modification for predicting the numbers at age in the year t_0-1 is as follows:

$$n_{a,t_0-1} = se^{-m(g+a-1)} c_{0,t_0-a-1} - \left(\sum_{i=1}^{a-1} e^{-m(i-1/2)} c_{a-i,t_0-i-1} \right) - e^{-m(a-1+g/2)} c_{0,t_0-a-1}$$

for $a = 2, \dots, A$

$n_{0,t_0-1} = sc_{0,t_0-1}$, and

$$n_{1,t_0-1} = se^{-(g)m} c_{0,t_0-2} - e^{-(g)m/2} c_{0,t_0-2}.$$

Maximum likelihood (equivalently non-linear least squares in this case) estimates of the parameters $v_1 = \log(m)$ and $v_2 = \log(s)$ were obtained using PROC IML in SAS applying the Newton-Raphson ridge optimization method. Survey estimates of pup production were given weights that are inversely proportional to their variance, and the predicted pup production was fit to the survey data.

Data Input

There are three sources of input data to obtain model estimates: pup surveys, catch-at-age, and age-specific pregnancy rates. There are currently seven independent estimates of pup production (Table 1). The model was fit to independent estimates of pup production in 1978, 1979, 1980 and 1983 based on mark-recapture experiments (Bowen and Sergeant, 1983, 1985; revised in Roff and Bowen 1986) and aerial survey estimates for 1990, 1994 and 1999 (Stenson *et al.* 1993, 1996, 2000b). The mark-recapture estimates were critically reviewed by Warren (1991), which also took into account Cooke *et al.*'s (1985) review of harp seal population dynamics.

A number of other estimates of pup production in Northwest Atlantic harp seals have been presented but were not included in the fitting procedure. For example, Bowen and Sergeant (1983) also presented the results of a mark-recapture experiment based on the 1977 marking of seals in the Gulf only. However, they concluded the estimates based on Gulf tags only ($318,000 \pm 48,000$) were likely to be negatively biased and so the estimates were not included. Similarly, Stenson *et al.* (1993) presented three estimates of pup production at the Front in 1990. However, one of these estimates was known to be incomplete while another was based on a series of flights made over two weeks and required a variety of assumptions to estimate ice drift over this period. Therefore, we used the 1990 pup production estimate of 577,900 (SE=38,000) based upon the visual surveys at the Front and photographic surveys in the Gulf (Stenson *et al.* 1993).

Attempts were made to estimate pup production using aerial surveys prior to 1990 but they could not be used to fit the model. Unfortunately none of the surveys carried out in 1950, 1951, 1955, 1959, 1960, 1975, 1977 and 1983 (Fisher 1952; Sergeant and Fisher 1960; Lavigne *et al.* 1980, 1982; Myers and Bowen 1989) covered all of the whelping concentrations in the Gulf and off Newfoundland in the same year. Also, none of the surveys covered the northern Gulf ('Mecatina') area, which can account for a significant number of pups in some years (e.g. see Stenson *et al.* 2000b). Given the larger variability in the proportion of pups born in the various whelping areas (Winters 1978; Stenson *et al.* 1996, 2000b) extrapolating the number of pups from one year to another is unreasonable. However, these surveys do provide minimum estimates of pup production for a number of years. Model estimates of pup production were greater than the partial survey estimates for all years where comparisons can be made (post-1960) in each of the model runs.

Using sequential population analysis a number of authors (e.g. Lett and Benjaminsen 1977; Winters 1978) estimated that pup production had declined from approximately 500,000 in the 1950s to approximately 300,000 – 350,000 in the 1970s. Unfortunately, the estimates of pup production are not independent of the assumed mortality and therefore, could not be used to fit to in this model.

Sergeant (1971, 1975), Benjaminsen and Øritsland (1975) and Winters (1978) used the survival index method to estimate average pup production for a various periods between the 1950s and 1970s. Cooke (1985) found that these earlier estimates were not accurate and revised this method to estimate pup production for the periods 1958 - 1967 (400,000 – 500,000) and 1968 – 1977 (300,000 – 400,000) depending upon differing assumptions of errors in the aging of samples. These estimates assume that pup production does not vary over the period being estimated and therefore were not be used in the current model.

The ‘catch’ data that are input to the model (Table 2; Figure 1) are not solely comprised of reported landings (Stenson *et al.* 2000a). These removals also include by-catches from the Newfoundland lump fishery (Walsh *et al.* 2000) and the eastern United States (Waring *et al.* 1999), and animals assumed struck and lost (Sjare and Stenson 2000). The associated rates of struck and lost used (Table 3) are based upon suggestions from the National Marine Mammal Peer Review Committee (Anon 1999b).

The pregnancy rate data used in this study (Table 4) are ‘harmonized’ pregnancy rates (Sjare *et al.* 2000) calculated using the methods of Warren *et al.* (1997). These data are available from 1954-1997. As such, we have assumed that the pregnancy rates in 1998 and 1999 are constant at the 1997 values. For periods in which there are no available data (e.g. 1971-77 for age 5), we have taken the average value of the pregnancy rates immediately prior to and following the gap.

Variance Estimates

As in the Cadigan-Shelton model, there is a statistical component in the current model. In this study the survey estimates are re-sampled to obtain approximate 95% confidence intervals for the pup and population trajectories, and the replacement yields, similar to Stenson *et al.* (1999), using the methods outlined in Warren *et al.* (1997). Calculating replacement yields for each of the estimated populations provides an approximate 95% C.I. for the estimated replacement yield.

The uncertainty in the population trajectory was estimated using the following re-sampling scheme. The set of pup production estimates were re-sampled 1000 times. The survey estimates of pup production in year t_i , \tilde{n}_{0,t_i} , are assumed to be normally distributed as:

$$\tilde{n}_{0,t_i} \sim N(n_{0,t_i}, \mathbf{S}_{t_i}),$$

where n_{0,t_i} is the true pup production for year t_i , and \mathbf{S}_{t_i} is the estimated variance of \tilde{n}_{0,t_i} . Furthermore, the re-sampled estimates of pup production, are assumed to be specified by the normal distribution:

$$\tilde{N}_{0,t_i} \sim N(\tilde{n}_{0,t_i}, \mathbf{S}_{t_i}).$$

To calculate replacement harvest, the estimated numbers-at-age for year 2000 were projected forward one year to 2001 using the 1999 estimates of pregnancy-at-age (see Table 4) in the year 2000. The catch in year 2000 was removed assuming the 1+ proportions-at-age from the catch (Table 5) were equal to the 1+ proportions-at-age in the reported landings plus by-catch in 1999 (Stenson *et al.*, 2000a). The average proportion of age-class 0 in reported catch plus by-catches from 1996-99 is 70%. In order to illustrate the impact of differing age structures, replacement yields were also estimated assuming 60% (average age composition from 1984-94) and also 80% pups (age composition of the recent catches in southern Canadian areas, respectively). The 2000 total catch was varied until the total population in

2001 equaled that in 2000. The impact of harvesting the harp seal population at these replacement yields for 5 and 10-year periods (i.e. up until 2005 and 2010) was also investigated.

The replacement yield reported here includes by-catch, struck and lost, and all reported catches in Canada and Greenland. In order to estimate the equivalent landed catch in the Canadian commercial harvest (i.e. Front and Gulf), we assumed that the levels of by-catch, struck and lost, Greenland catches and Arctic catches were the same as in 1999. We adjust the calculated replacement yields by these amounts and present the replacement yields in units of Canadian Front and Gulf catch. If the levels of the other removals change, they will impact the estimated Canadian Front and Gulf landings that will achieve the replacement harvest.

Results and Discussion

The rate of unreported mortality (m) can be a difficult parameter to estimate in animal populations. Independent estimates of the age structure of the population are difficult to obtain due to potential biases in sampling (e.g. Sergeant 1975; Roff and Bowen 1986) and changes in recruitment and hunting mortality. Roff and Bowen (1983) reviewed the available data on mortality rates of harp seals. They concluded that although there was conflicting evidence about the relative levels of mortality among young of the year and older seals, it was prudent to assume some level of higher mortality among first year animals. The level of mortality that occurs among young seals is not known, but Roff and Bowen (1983, 1986), Shelton *et al.* (1992, 1996) and Stenson *et al.* (1999) assumed that mortality during the first year was 3 times that of older seals. This assumption was also used to estimate population size and sustainable yields of Greenland Sea and White Sea / Barents Sea harp seals (Anon 1999a). We attempted to estimate mortality of young of the year as a multiple of the mortality of older seals (γ), but were unable to fit a 3-parameter model to the limited data available on pup production. It is likely impossible to estimate γ (due to confounding) in this model given that the model is fitting to pup production and that we also estimate unreported mortality m . For the 'base case' we use $\gamma = 3$ to make our results comparable to earlier studies. The results obtained when re-sampling the survey data are restricted to the $\gamma = 3$ case.

Anon. (1999a) also examined the impact of assuming that mortality among young seals in the White Sea is higher (5 times that of 1+ seals). In order to investigate the impact of the assumed level of mortality among first year animals, we varied the multiplier used (γ) between 1 (constant mortality for all ages), 3 and 5. Model runs indicate that there is very little difference in predicted pup production (Figure 2; Table 6) for $\gamma = 1, 3,$ and $5,$ not surprising considering that the data used in fitting are pup production estimates. Population trajectories also exhibit similar trends, but population size differs slightly for each of the gamma values (Figure 3; Table 7). In the year 2000, the predicted pup production of the three model runs range from 836,000 to 848,000 and the predicted population sizes are approximately 5.41M, 5.22M, and 5.09M for $\gamma = 1, 3,$ and $5,$ respectively. Parameter estimates and likelihood values (negative maximum likelihood) corresponding to these estimates are presented in Table 8. Even though the fit improves as γ increases, the (profile) likelihood ratio test indicates that no pair of estimates are significantly different. For $\gamma = 3,$ the mortality estimate indicates that 84% of pups will survive their first year of life, and that the annual survival rate of older cohorts is 94%.

The pup production estimates show that following a slight decline in the mid 1960's to 1970, the population has produced pups at a rate that has increased almost steadily since this period. Some aberrations exist, a result of the declining pregnancy rates (which change abruptly). Using smoother pregnancy rates should result in less 'sharp' changes in the estimated pup production.

The population trajectory also shows a pattern of growth since the mid 1960's but only up to the mid 1990s. Unlike pup production, total population seems to have stabilized at slightly over 5 million since about 1996. Figure 4 shows the results of 988 population trajectories estimated by the 1000 re-sampled the pup production estimates (12 model fits failed to converge) for the base case ($\gamma = 3$). The distribution of population sizes in the year 2000 is presented in Figure 5. The mean estimated population size in the year 2000 for this scenario is 5,215,000 with asymptotic 95% confidence interval of 4,022,000 to 6,408,000. This resampling process only accounts for the error in the pup production estimates. As such, the estimated variance and confidence intervals are likely to be underestimated. When the error associated with estimating pregnancy rates is included in the resampling process,

the asymptotic confidence intervals will likely expand by only a small amount (Warren *et al.* (1997) and Healey and Stenson (unpublished)).

Based on comparison of the 1996 and 2000 population estimates for each of the 988 trajectories given in Figure 4, the average change in population size over these four years has been -0.7% (95% C.I. $-9.9 - 7.7\%$), which is not significantly different from zero (i.e. no discernable change in population size). During this same period pup production increased by an average of 13.0% (95% C.I. $5.7 - 20.0\%$). This difference arises since the large catch of young observed in the past four years has not yet impacted the breeding population. It will do so when cohorts mature, at approximately age 5 (i.e. starting in 2001) (Sjare *et al.*, 2000).

Estimates of sustainable yield require accurate predictions of reproductive rates and the age structure of the harvest over extended periods of time. These are unlikely to be constant and therefore the use of sustainable yields to determine harvest quotas is questionable. Replacement yields do not require these predictions to extend beyond the near term and therefore, the sensitivity of these predictions on the long-term sustainability of the population is diminished. However, it is important to monitor the annual removals and re-estimate replacement yield on a regular basis.

The replacement yields, and the resultant population sizes in 2005 and 2010 if the replacement yields are harvested in the intervening period are presented for various scenarios in Table 9. The replacement yield reported here includes reported catches in Canada and Greenland, by-catch, and struck and lost. Under the base case of $\gamma = 3$, the replacement yields are 522,000, 531,000, and 541,000 if the proportion of young in the catch is 0.6, 0.7, or 0.8, respectively (Table 9). The frequency distribution of replacement yields corresponding to each of the populations shown in Figure 4 is given in Figure 6. Assuming that 70% of the removals consist of age class 0 animals, the mean replacement yield is 533,000, 95% C.I.: (373,000, 693,000).

To project the impact of this assumption on future populations, we have assumed future pregnancy rates and the 1+ age structure of the catch will be constant at their 1999 levels. If the proportion of age class 0's taken by all components of removals is 60%, then continued removals at the replacement yield level will cause the population to decrease slightly over the next 5 to 10 years. However, if the overall proportion of the age 0 group taken is 0.8 (resulting in fewer older reproducing animals being harvested), then the population size will increase. At the current level of approximately 70% age class 0, the population will remain relatively stable.

In order to estimate the portion of the replacement yield that will become landed catch in the Canadian commercial harvest, we assumed that the levels of catches in Greenland and in the Canadian Arctic, struck and loss associated with these harvests and by-catch were the same as in 1999. We adjust the calculated replacement yields by these amounts and present the replacement yields in units of Canadian Front and Gulf landings. The proportion of young in the Canadian commercial harvest was varied from 70% to 90% to illustrate the impact of changes in the age structure on the replacement yields. The situation for which the overall proportion of age 0's taken from all hunt components is 70% and the Canadian Front and Gulf harvest is 90% closely matches the data for 1999 (the Canadian Front and Gulf actually took over 95% pups in 1999). Using these assumptions, the replacement yield was estimated to be 531,000, with a corresponding Canadian Front and Gulf yield 257,000, 95% C.I. (102,000, 342,000). If the levels of the northern catches or by-catch change, they will naturally impact the estimated Canadian Front and Gulf landings that will achieve the replacement harvest.

In summary, the results indicate that the estimated population size of the northwest Atlantic harp seal herd is approximately 5.2 million, and the population has been stable at this level for the past few years. Total pup production has been generally increasing since the mid-1970's. In the coming years the rate of increase is expected to slow as the large pup catches taken since 1996 begin to affect the breeding population.

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Table 1: Pup production surveys used to estimate pup production

| Year | Estimate | Standard Error | Reference |
|------|----------|----------------|-----------------------------|
| 1978 | 497000 | 34000 | Roff and Bowen 1986 |
| 1979 | 478000 | 35000 | Roff and Bowen 1986 |
| 1980 | 475000 | 47000 | Roff and Bowen 1986 |
| 1983 | 534000 | 33000 | Bowen and Sergeant 1985 |
| 1990 | 577900 | 38800 | Stenson <i>et al.</i> 1993 |
| 1994 | 702900 | 63600 | Stenson <i>et al.</i> 1996 |
| 1999 | 997900 | 102100 | Stenson <i>et al.</i> 2000b |

Table 2: Total removals of northwest Atlantic harp seals (reported landings + by-catch + struck & lost), 1952-1999.

| Year | Age | | | | | | | | | | | | | Total |
|------|--------|-------|-------|-------|-------|-------|-------|------|------|------|-------|------|-------|--------|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12+ | |
| 1952 | 219536 | 10876 | 13941 | 9642 | 7359 | 7771 | 12593 | 8684 | 8456 | 6238 | 7130 | 5955 | 28398 | 346579 |
| 1953 | 219447 | 26292 | 8458 | 7595 | 5086 | 4924 | 4086 | 3368 | 3373 | 3231 | 2840 | 3160 | 20152 | 312012 |
| 1954 | 199519 | 38327 | 15053 | 5993 | 7151 | 3920 | 4686 | 3932 | 3584 | 2512 | 3478 | 1572 | 19229 | 308956 |
| 1955 | 273296 | 27225 | 10561 | 7776 | 5617 | 4841 | 4484 | 3641 | 3749 | 3033 | 3440 | 2916 | 20793 | 371372 |
| 1956 | 357914 | 15935 | 6365 | 4682 | 3634 | 2845 | 2761 | 2334 | 2415 | 2083 | 2234 | 1827 | 13828 | 418857 |
| 1957 | 182432 | 26232 | 9775 | 6887 | 5411 | 4328 | 4188 | 3543 | 3551 | 3067 | 3436 | 3034 | 21413 | 277297 |
| 1958 | 162465 | 30211 | 12029 | 13248 | 13308 | 11059 | 7505 | 6648 | 5615 | 5297 | 10263 | 6089 | 54395 | 338132 |
| 1959 | 251899 | 25194 | 9584 | 6699 | 5137 | 4373 | 4310 | 3629 | 3592 | 3135 | 3478 | 2925 | 20834 | 344789 |
| 1960 | 176927 | 38286 | 14839 | 11380 | 7894 | 6453 | 6447 | 5187 | 5008 | 4320 | 4930 | 4213 | 30142 | 316026 |
| 1961 | 184800 | 9159 | 3621 | 3402 | 3463 | 1488 | 1678 | 1445 | 997 | 930 | 1316 | 782 | 4243 | 217324 |
| 1962 | 219330 | 32755 | 35492 | 10658 | 9642 | 6765 | 3218 | 2869 | 2898 | 2828 | 1422 | 1453 | 14459 | 343789 |
| 1963 | 284999 | 11568 | 10023 | 7963 | 4807 | 3841 | 4054 | 4035 | 3730 | 3427 | 3983 | 3742 | 23113 | 369285 |
| 1964 | 279868 | 8001 | 7018 | 6965 | 7499 | 5119 | 7119 | 3963 | 3135 | 2944 | 4490 | 2408 | 28559 | 367088 |
| 1965 | 195499 | 14106 | 7161 | 5883 | 5828 | 6776 | 6138 | 2673 | 1299 | 932 | 1587 | 638 | 10246 | 258766 |
| 1966 | 261978 | 15451 | 12172 | 5987 | 5583 | 5651 | 5527 | 5078 | 3397 | 1886 | 2022 | 2459 | 16894 | 344085 |
| 1967 | 285596 | 15430 | 7430 | 3389 | 2801 | 3593 | 4340 | 3812 | 2649 | 1766 | 1658 | 1980 | 15342 | 349786 |
| 1968 | 166413 | 7605 | 5657 | 3870 | 2417 | 2103 | 1978 | 2622 | 2530 | 1780 | 1845 | 1374 | 12251 | 212445 |
| 1969 | 243285 | 22981 | 4169 | 3875 | 3083 | 3263 | 2414 | 2727 | 3107 | 2304 | 2036 | 1751 | 13178 | 308173 |
| 1970 | 226503 | 9914 | 8405 | 3787 | 3181 | 3085 | 1855 | 1930 | 1956 | 1854 | 2295 | 1609 | 10068 | 276442 |
| 1971 | 220822 | 9356 | 3617 | 3423 | 1677 | 1412 | 974 | 788 | 664 | 991 | 983 | 786 | 4224 | 249717 |
| 1972 | 126199 | 6148 | 3840 | 2362 | 2305 | 1125 | 962 | 843 | 522 | 270 | 445 | 414 | 3500 | 148935 |
| 1973 | 110548 | 9313 | 5953 | 4040 | 2897 | 3835 | 1379 | 1220 | 1333 | 781 | 875 | 931 | 5604 | 148709 |
| 1974 | 125659 | 13542 | 7337 | 2744 | 2314 | 2095 | 3037 | 1045 | 1112 | 1188 | 877 | 682 | 5992 | 167624 |
| 1975 | 151069 | 16419 | 7701 | 3957 | 2239 | 1844 | 1644 | 1641 | 983 | 772 | 1024 | 671 | 4232 | 194196 |

Table 2. Continued

| Year | Age | | | | | | | | | | | | | Total |
|------|--------|-------|-------|-------|-------|-------|-------|------|------|------|------|------|-------|--------|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12+ | |
| 1976 | 150261 | 20935 | 10085 | 5497 | 3473 | 1185 | 799 | 745 | 767 | 337 | 559 | 442 | 2810 | 197895 |
| 1977 | 151496 | 11394 | 7774 | 6560 | 4753 | 2385 | 1362 | 1094 | 688 | 336 | 454 | 435 | 2898 | 191629 |
| 1978 | 136172 | 27319 | 14993 | 9283 | 5934 | 4033 | 3010 | 997 | 1352 | 594 | 926 | 458 | 3811 | 208882 |
| 1979 | 156317 | 22747 | 11646 | 5995 | 3358 | 2226 | 1708 | 1152 | 780 | 616 | 502 | 355 | 4518 | 211920 |
| 1980 | 144697 | 25954 | 12943 | 9090 | 5049 | 3411 | 2655 | 2028 | 1582 | 1083 | 937 | 998 | 7368 | 217795 |
| 1981 | 196515 | 22477 | 11404 | 8692 | 5660 | 4104 | 2856 | 1926 | 1541 | 814 | 1017 | 1001 | 6835 | 264842 |
| 1982 | 167498 | 23830 | 14302 | 8694 | 4539 | 3259 | 1954 | 1877 | 1293 | 1681 | 1293 | 1022 | 5949 | 237191 |
| 1983 | 69499 | 18548 | 9220 | 6990 | 5051 | 2454 | 2276 | 1960 | 931 | 1056 | 1043 | 750 | 4954 | 124732 |
| 1984 | 36460 | 11362 | 11983 | 10284 | 6132 | 4016 | 3073 | 2513 | 1961 | 971 | 1105 | 1058 | 8907 | 99825 |
| 1985 | 25777 | 10245 | 9881 | 8981 | 5081 | 3315 | 2574 | 2078 | 1746 | 850 | 1019 | 770 | 7450 | 79767 |
| 1986 | 40913 | 12506 | 11120 | 10873 | 5982 | 3879 | 3025 | 2397 | 1964 | 1022 | 1090 | 1008 | 9125 | 104904 |
| 1987 | 66411 | 17985 | 16143 | 16201 | 9763 | 6148 | 4760 | 3565 | 3053 | 1642 | 1666 | 1578 | 13529 | 162444 |
| 1988 | 92908 | 23563 | 21742 | 19129 | 11269 | 6978 | 5079 | 3769 | 3319 | 1534 | 1530 | 1334 | 15016 | 207170 |
| 1989 | 75550 | 17477 | 15847 | 15313 | 9475 | 6466 | 4744 | 3495 | 2909 | 1451 | 1459 | 1323 | 13006 | 168515 |
| 1990 | 49985 | 21659 | 19199 | 20162 | 12090 | 8057 | 5590 | 3984 | 3044 | 1641 | 1752 | 1711 | 15197 | 164071 |
| 1991 | 65607 | 19701 | 16160 | 16508 | 10667 | 7751 | 5535 | 3995 | 3276 | 1598 | 1706 | 1753 | 14447 | 168704 |
| 1992 | 70003 | 26669 | 21685 | 19015 | 12119 | 8439 | 6793 | 5292 | 3782 | 2473 | 2034 | 1806 | 16362 | 196472 |
| 1993 | 57944 | 23585 | 19537 | 18507 | 10837 | 7625 | 5922 | 4552 | 3738 | 1912 | 1827 | 1690 | 15171 | 172847 |
| 1994 | 70227 | 28998 | 24014 | 24697 | 16673 | 11325 | 8715 | 6293 | 5679 | 3030 | 2678 | 2689 | 22017 | 227035 |
| 1995 | 59028 | 33521 | 27826 | 26307 | 16074 | 12513 | 8960 | 7582 | 5248 | 2641 | 2398 | 2457 | 21560 | 226115 |
| 1996 | 219087 | 48683 | 39473 | 30427 | 18458 | 13419 | 10334 | 8504 | 6741 | 3460 | 4030 | 3764 | 35775 | 442155 |
| 1997 | 257129 | 47907 | 33296 | 26759 | 15778 | 11083 | 8558 | 6796 | 5540 | 2678 | 3679 | 3120 | 25004 | 447327 |
| 1998 | 289592 | 39448 | 30127 | 29757 | 17136 | 14079 | 11075 | 8752 | 8219 | 4347 | 3566 | 3962 | 28866 | 488926 |
| 1999 | 280819 | 41801 | 34454 | 32655 | 18839 | 13341 | 10238 | 7974 | 6841 | 3158 | 3215 | 3094 | 26985 | 483414 |

Table 3: Assumed levels of struck and lost for young of year (0) and older (1+) seals.

| | Harvest Area | | | |
|-----------|----------------|-----|---------------------------|-----|
| | Front and Gulf | | Can. Arctic and Greenland | |
| | 0 | 1+ | 0 | 1+ |
| 1952-1982 | 0.01 | 0.5 | 0.5 | 0.5 |
| 1983-1999 | 0.05 | 0.5 | 0.5 | 0.5 |

Table 4: Harmonized pregnancy rates used in the model (Sjare *et al.* 2000).

| Year | Age 4 | Age 5 | Age 6 | Age 7 | Age 8+ |
|------|--------|--------|--------|--------|--------|
| 1954 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1955 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1956 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1957 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1958 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1959 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1960 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1961 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1962 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1963 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1964 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1965 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1966 | 0.0192 | 0.1818 | 0.5435 | 0.7231 | 0.874 |
| 1967 | 0.0192 | 0.1818 | 0.5435 | 0.9512 | 0.874 |
| 1968 | 0.0192 | 0.1818 | 0.5435 | 0.9512 | 0.874 |
| 1969 | 0.0192 | 0.1818 | 0.5435 | 0.8143 | 0.874 |
| 1970 | 0.0192 | 0.1818 | 0.5435 | 0.8143 | 0.874 |
| 1971 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1972 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1973 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1974 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1975 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1976 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1977 | 0.0192 | 0.3834 | 0.7162 | 0.8143 | 0.874 |
| 1978 | 0.0192 | 0.5849 | 0.8889 | 0.8143 | 0.874 |
| 1979 | 0.1395 | 0.5849 | 0.8889 | 0.8143 | 0.874 |
| 1980 | 0.1395 | 0.5849 | 0.8889 | 0.8143 | 0.874 |
| 1981 | 0.1395 | 0.5849 | 0.8889 | 0.8143 | 0.874 |
| 1982 | 0.1395 | 0.2054 | 0.8889 | 0.8143 | 0.7763 |
| 1983 | 0.1395 | 0.2054 | 0.7172 | 0.8143 | 0.7763 |
| 1984 | 0.1395 | 0.2054 | 0.7172 | 0.8143 | 0.7763 |
| 1985 | 0.1395 | 0.2054 | 0.5455 | 0.8143 | 0.7763 |
| 1986 | 0.1395 | 0.2054 | 0.5455 | 0.8143 | 0.7763 |
| 1987 | 0.1395 | 0.2054 | 0.5455 | 0.8143 | 0.7763 |
| 1988 | 0.1395 | 0.2054 | 0.5455 | 0.6866 | 0.7763 |
| 1989 | 0.1395 | 0.2054 | 0.5455 | 0.5588 | 0.7763 |
| 1990 | 0.1395 | 0.2054 | 0.5455 | 0.5588 | 0.6456 |
| 1991 | 0.1395 | 0.2054 | 0.5455 | 0.5588 | 0.6456 |
| 1992 | 0.1395 | 0.2054 | 0.5455 | 0.5588 | 0.6456 |
| 1993 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1994 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1995 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1996 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1997 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1998 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |
| 1999 | 0.0377 | 0.2054 | 0.3103 | 0.5588 | 0.6456 |

Table 5. Catch proportion-at-age used to calculate replacement yields. Values of β examined equal 0.6, 0.7, and 0.8.

| Age | Proportion of Catch |
|-----|------------------------|
| 0 | β |
| 1 | $(1-\beta) * (0.2133)$ |
| 2 | $(1-\beta) * (0.1665)$ |
| 3 | $(1-\beta) * (0.1501)$ |
| 4 | $(1-\beta) * (0.0876)$ |
| 5 | $(1-\beta) * (0.0647)$ |
| 6 | $(1-\beta) * (0.0502)$ |
| 7 | $(1-\beta) * (0.0398)$ |
| 8 | $(1-\beta) * (0.0344)$ |
| 9 | $(1-\beta) * (0.0171)$ |
| 10 | $(1-\beta) * (0.0177)$ |
| 11 | $(1-\beta) * (0.0171)$ |
| 12+ | $(1-\beta) * (0.1414)$ |

Table 6: Estimated pup production for northwest Atlantic harp seals, 1960-2000.

| Year | Survey | $\gamma=1$ | $\gamma=3$ | $\gamma=5$ |
|------|--------|------------|------------|------------|
| 1960 | | 349510.8 | 352755.6 | 354672.5 |
| 1961 | | 358463.2 | 361895.5 | 363971.1 |
| 1962 | | 372549.3 | 376465.9 | 378967.6 |
| 1963 | | 410456.7 | 415169.7 | 418315.5 |
| 1964 | | 422294.6 | 428686.9 | 433098.8 |
| 1965 | | 421779.9 | 429798.4 | 435456.1 |
| 1966 | | 413129 | 422095.5 | 428514 |
| 1967 | | 407304.3 | 416348.6 | 422856.9 |
| 1968 | | 400118.8 | 407590.5 | 412937.7 |
| 1969 | | 387205.6 | 393815.3 | 398537.7 |
| 1970 | | 373905.2 | 380262 | 384830 |
| 1971 | | 367368.8 | 372796.9 | 376686.8 |
| 1972 | | 388048.7 | 391112.5 | 393257.5 |
| 1973 | | 389087.5 | 392272.9 | 394478.4 |
| 1974 | | 400121.1 | 403278.8 | 405444.6 |
| 1975 | | 406587.9 | 409808.5 | 412008.7 |
| 1976 | | 407468.6 | 410893.8 | 413245.9 |
| 1977 | | 410421.1 | 414003.3 | 416486.2 |
| 1978 | 497000 | 428681.4 | 431863.2 | 434091.7 |
| 1979 | 478000 | 487721 | 488026.4 | 488221.5 |
| 1980 | 475000 | 524036.2 | 522849.4 | 521997.9 |
| 1981 | | 546908.5 | 545439.9 | 544377.4 |
| 1982 | | 562896.2 | 561391.6 | 560289.5 |
| 1983 | 534000 | 505664.9 | 505433.5 | 505204 |
| 1984 | | 509226 | 509700.1 | 509992.9 |
| 1985 | | 533774 | 533587.9 | 533437.1 |
| 1986 | | 545865 | 545667.9 | 545562.9 |
| 1987 | | 580260.8 | 578405.9 | 577167.4 |
| 1988 | | 615369.2 | 612174.1 | 609997 |
| 1989 | | 637948.3 | 634809.7 | 632669.5 |
| 1990 | 577900 | 665012.2 | 662771.2 | 661236.2 |
| 1991 | | 620408.4 | 616684.6 | 614040.6 |
| 1992 | | 657817.6 | 654555.8 | 652219.3 |
| 1993 | | 693070.4 | 690307.2 | 688330.6 |
| 1994 | 702900 | 676163 | 677873.3 | 679046.7 |
| 1995 | | 710795.2 | 712910.9 | 714409.3 |
| 1996 | | 741398.8 | 743890.8 | 745697.3 |
| 1997 | | 770117 | 773187.3 | 775443.4 |
| 1998 | | 793280.8 | 797022.8 | 799789.9 |
| 1999 | 997900 | 818212.2 | 822719.1 | 826062.1 |
| 2000 | | 836338.8 | 841871.2 | 845958.4 |

Table 7: Estimated population size for northwest Atlantic harp seals, 1960-2000.

| Year | $\gamma=1$ | $\gamma=3$ | $\gamma=5$ |
|------|------------|------------|------------|
| 1960 | 2143954 | 2083793 | 2042732 |
| 1961 | 2052085 | 1993559 | 1953586 |
| 1962 | 2075827 | 2018362 | 1979182 |
| 1963 | 2013760 | 1958023 | 1920166 |
| 1964 | 1943115 | 1889456 | 1853267 |
| 1965 | 1878862 | 1826338 | 1791109 |
| 1966 | 1914901 | 1859538 | 1822421 |
| 1967 | 1860294 | 1806709 | 1770734 |
| 1968 | 1796696 | 1744483 | 1709279 |
| 1969 | 1857103 | 1799744 | 1760984 |
| 1970 | 1807685 | 1751011 | 1712745 |
| 1971 | 1785717 | 1728882 | 1690480 |
| 1972 | 1811720 | 1752742 | 1712817 |
| 1973 | 1934309 | 1867168 | 1821879 |
| 1974 | 2059846 | 1985340 | 1935116 |
| 1975 | 2165086 | 2084653 | 2030436 |
| 1976 | 2238424 | 2154332 | 2097645 |
| 1977 | 2306177 | 2219416 | 2160908 |
| 1978 | 2393653 | 2304497 | 2244343 |
| 1979 | 2517585 | 2421455 | 2356522 |
| 1980 | 2666508 | 2558916 | 2486533 |
| 1981 | 2822545 | 2701198 | 2619900 |
| 1982 | 2938575 | 2806169 | 2717720 |
| 1983 | 3016214 | 2872822 | 2777173 |
| 1984 | 3200740 | 3049598 | 2948575 |
| 1985 | 3421367 | 3262156 | 3155411 |
| 1986 | 3658513 | 3491139 | 3378754 |
| 1987 | 3889721 | 3715028 | 3597559 |
| 1988 | 4084822 | 3902095 | 3779272 |
| 1989 | 4246106 | 4055692 | 3927932 |
| 1990 | 4460854 | 4262765 | 4130033 |
| 1991 | 4620745 | 4411996 | 4272049 |
| 1992 | 4802745 | 4591788 | 4450396 |
| 1993 | 4980859 | 4766458 | 4622840 |
| 1994 | 5152814 | 4937343 | 4793223 |
| 1995 | 5295437 | 5082912 | 4940532 |
| 1996 | 5459894 | 5247833 | 5105651 |
| 1997 | 5433334 | 5228467 | 5091243 |
| 1998 | 5426743 | 5228064 | 5095242 |
| 1999 | 5405362 | 5212286 | 5083560 |
| 2000 | 5408879 | 5218753 | 5092357 |

Table 8: Estimated parameter values (from estimates of $\log(m)$ and $\log(s)$).

| | m | γm | s | Likelihood |
|------------|----------|------------|----------|------------|
| $\gamma=1$ | 0.070124 | - | 2.151185 | 14.26 |
| $\gamma=3$ | 0.058425 | 0.175275 | 2.226661 | 13.42 |
| $\gamma=5$ | 0.050211 | 0.260055 | 2.284662 | 12.86 |

Table 9: Replacement yields (in units of 'total removals'), corresponding Canadian Front and Gulf Harvest (assuming $\gamma = 3$), and population sizes if the replacement yield is taken for 5 or 10 years, for various age structures of future catch.

| Age 0 % (Overall) | Replacement Yield | Age 0% (Cdn. F&G) | Cdn. F&G Landings | Pop'n in 2005 (millions) | Pop'n in 2010 (millions) |
|----------------------|----------------------|----------------------|----------------------|-----------------------------|-----------------------------|
| 0.6 | 522,000 | 0.7 | 213,000 | 5.19 | 5.08 |
| | | 0.8 | 230,000 | | |
| | | 0.9 | 249,000 | | |
| 0.7 [†] | 531,000 | 0.7 | 220,000 | 5.25 | 5.28 |
| | | 0.8 | 237,000 | | |
| | | 0.9 [†] | 257,000 | | |
| 0.8 | 541,000 | 0.7 | 228,000 | 5.32 | 5.49 |
| | | 0.8 | 225,000 | | |
| | | 0.9 | 265,000 | | |

[†] = Similar to 1999 Proportions

Total Removals of NW Atlantic Harp Seals, 1952-1999

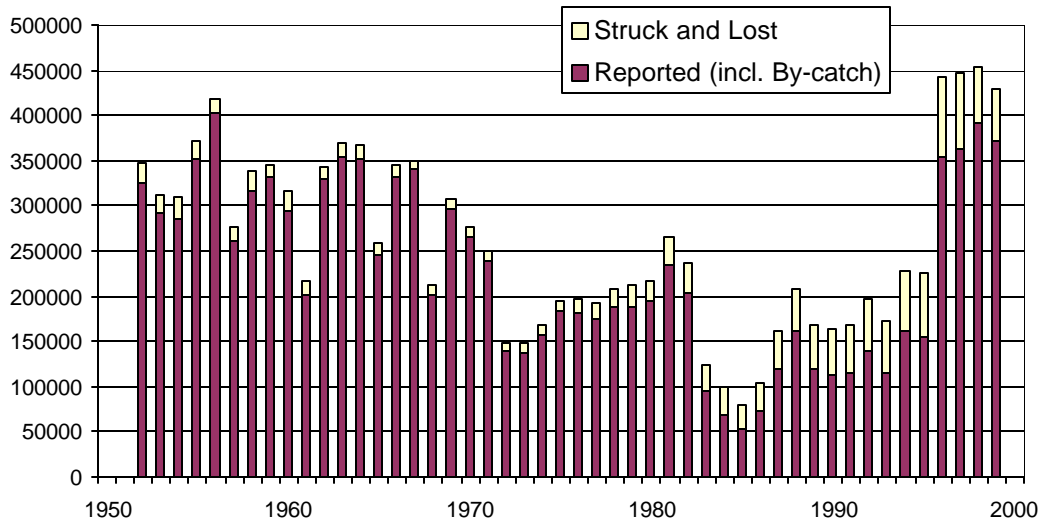


Figure 1: Total removals (reported landings+ by-catch + struck & lost) of Northwest Atlantic harp seals, 1952-1999.

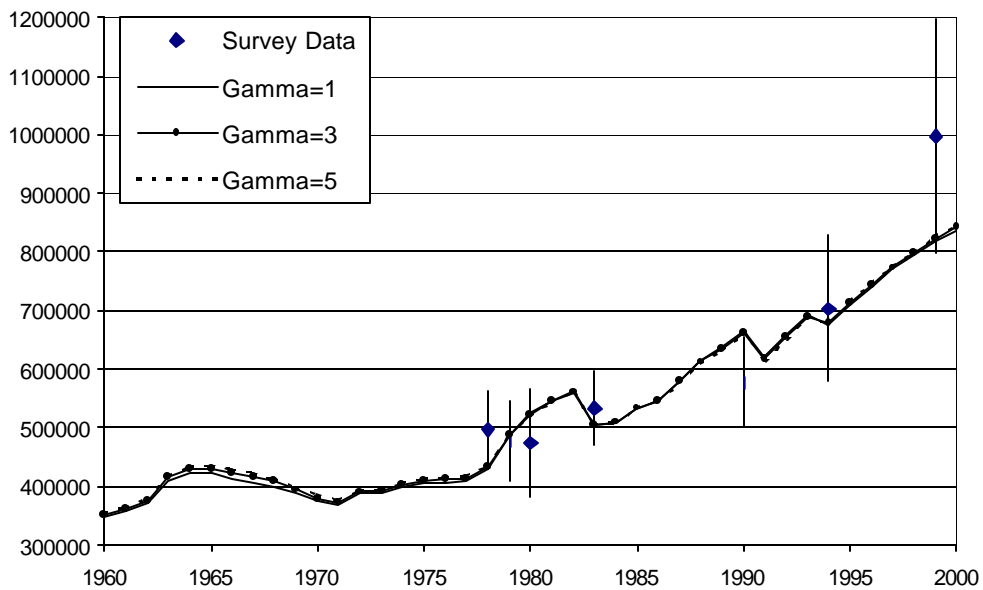


Figure 2: Estimated pup production of northwest Atlantic harp seals under three differing assumptions for first year mortality (γ), survey estimates of pup production, and asymptotic 95% C.I.'s for the survey estimates.

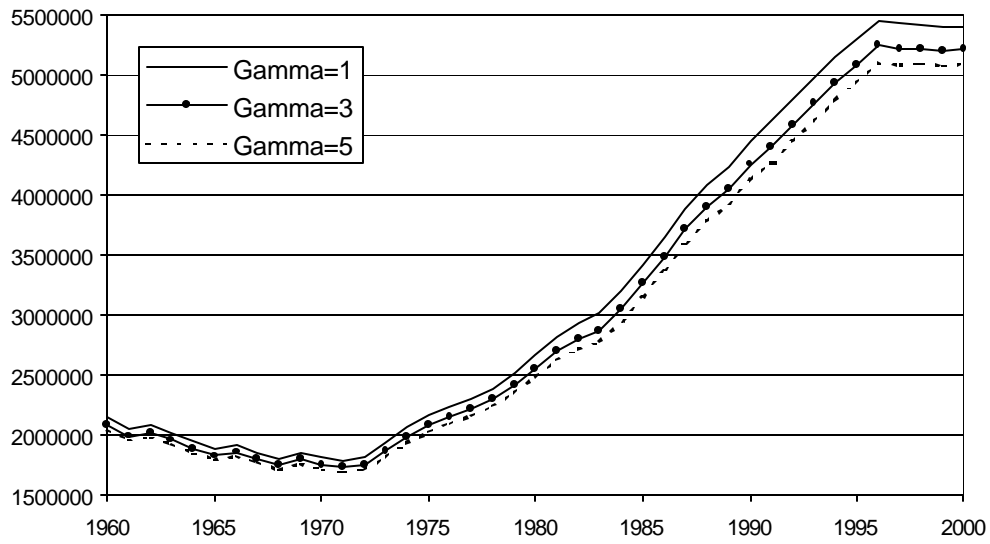


Figure 3: Estimated population size of northwest Atlantic harp seals under three differing assumptions for first year mortality (Γ).

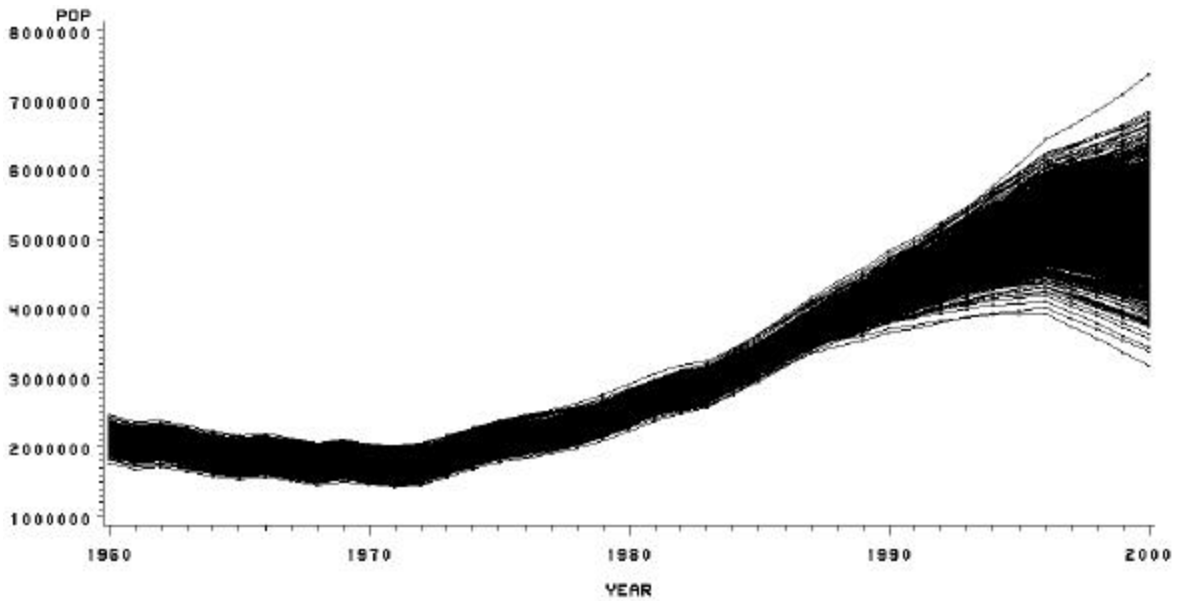


Figure 4: Population trajectories of northwest Atlantic harp seals estimated by 1000 resamplings of estimated pup production.

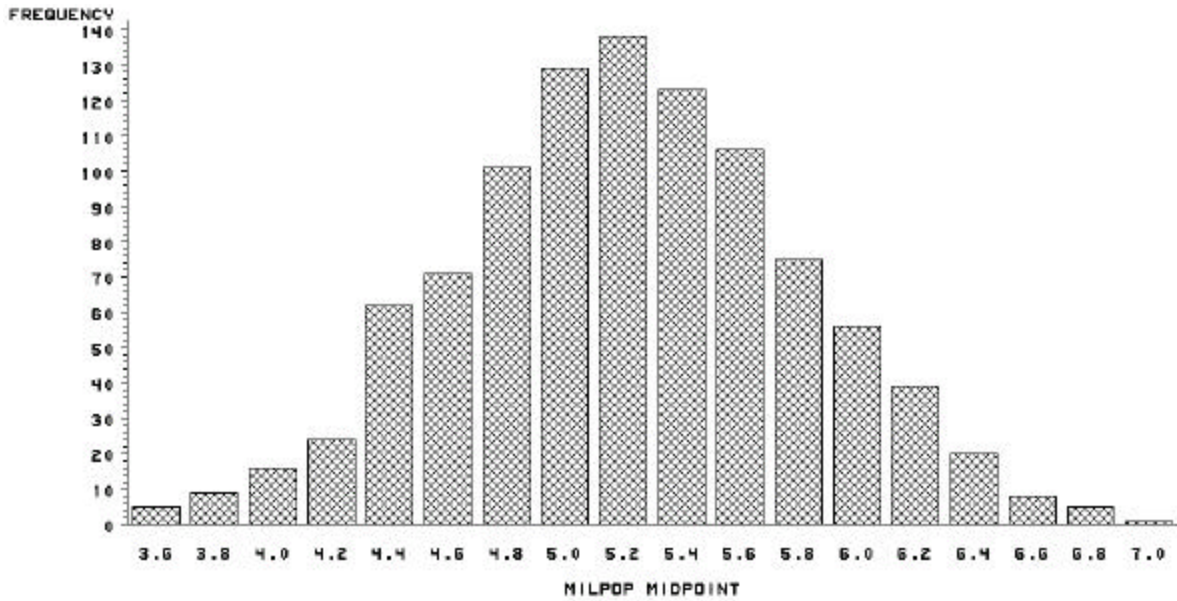


Figure 5: Frequency distribution of estimated population sizes in 2000 based upon 1000 resamplings of pup production estimates. Mean population = 5,215,000 (SE=596,000).

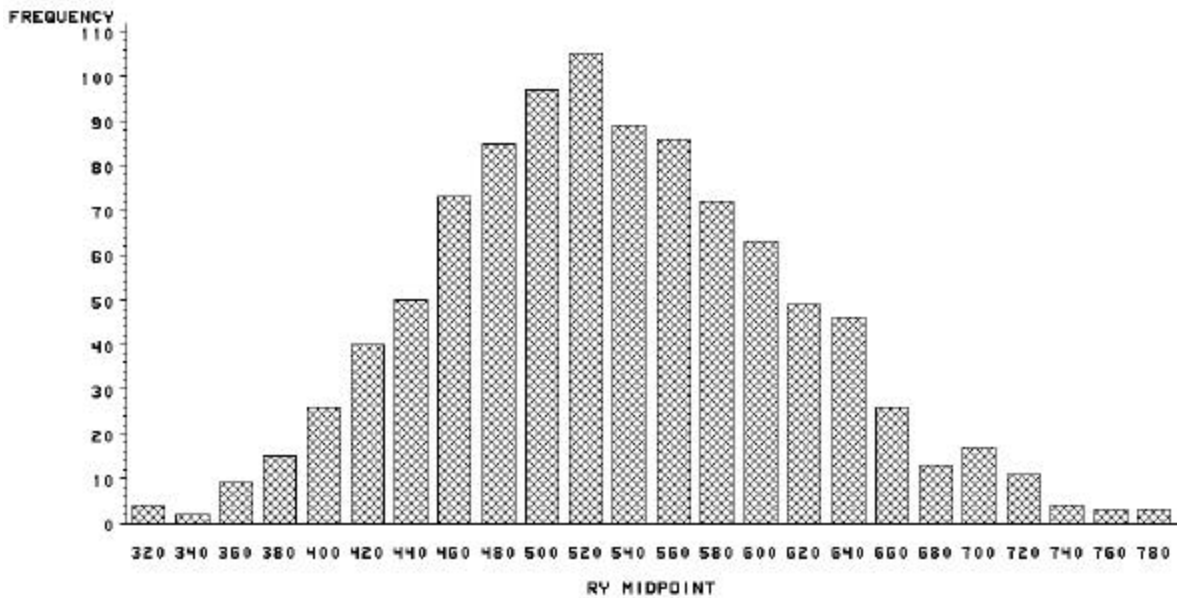


Figure 6: Frequency distribution of estimated replacement yields based upon 1000 resamplings of estimated pup production assuming $\gamma=3$ and 70% of the total removals consist of age class 0. Mean RY = 533,000 (SE=82,000).